## B.TECH SYLLABUS

## DEPARTMENT OF MATHEMATICS

## Engineering Mathematics I

COURSE CODE: 18B11MA111
COURSE CREDITS: 4
CORE/ELECTIVE: CORE
L-T-P: 3-1-0

Pre-requisite: Basic concepts of calculus and algebra

## Course Objectives:

1. Various techniques of Multivariate Calculus and Integral Calculus.
2. The fundamental concepts of Vector Calculus.
3. The fundamentals of Laplace transforms and their applications.
4. To develop the essential tool of Matrices and Linear Algebra in a comprehensive manner.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Evaluate partial derivatives with its physical significance and expand <br> functions of several variables. |  <br> Usage |
| CO-2 | Find maxima and minima of functions of several variables with <br> without constraints. | Assessment |
| CO-3 | Find areas and volumes of solids using multiple integration | Assessment |
| CO-4 | Understand the calculus of vectors and vector valued functions <br> with their physical significance |  |
| Usage |  |  |$⿻$| Usage |  |  |  |
| :---: | :---: | :---: | :---: |
| CO-5 | Use Laplace transforms and inverse Laplace transforms to <br> solve IVP | Solve linear systems of equations and perform diagonalization <br> of matrices | Usage |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Differential Calculus: Limits and continuity of function, Partial <br> Differentiation, Chain rule, Total Derivative; Maxima, Minima and <br> Saddle points; Method of Lagrange's multipliers, Taylor's series for two <br> or more variables | $\mathbf{1 0}$ |


| $\mathbf{2}$ | Integral Calculus: Improper integrals; Beta and Gamma functions and <br> their properties; Double integrals, Change of order and Change of <br> variables, Applications to areas and volumes. | $\mathbf{1 0}$ |
| :---: | :--- | :---: |
| $\mathbf{3}$ | Vector Calculus: Equations to a line and a plane, Tangent plane and <br> Normal line, Gradient, Curl and divergence and their physical <br> significance, Directional derivatives, Line and surface integrals. | $\mathbf{6}$ |
| $\mathbf{4}$ | Laplace Transform: Laplace Transform, Inverse Laplace transform, <br> Convolution, Dirac delta and Unit Step function, Solution of initial value <br> problems. | $\mathbf{6}$ |
| $\mathbf{5}$ | Matrices: Algebra of matrices, Row Echelon form, Inverse and Rank of <br> a matrix, Symmetric, Skew- symmetric and Orthogonal matrices; <br> Determinants; Solution of systems of linear equations (Gauss's <br> elimination, Rank method, Linear Independence and Dependence of <br> vectors. Eigen values and Eigenvectors; Cayley-Hamilton Theorem, <br> Diagonalization of matrices and Orthogonal transformation. | $\mathbf{1 0}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. G.B. Thomas and R.L. Finney, Calculus and Analytic geometry, 9th Edition, Pearson, 2002.
2. Erwin Kreyszig, Advanced Engineering Mathematics, 9th Edition, John Wiley \& Sons, 2006.
3. Jain and Iyengar, Advanced Engineering Mathematics, Narosa Publishing House.

## Suggested Reference Book(s):

1. Ramana B.V., Higher Engineering Mathematics, Tata McGraw Hill New Delhi, 11thReprint, 2010.
2. D. Poole, Linear Algebra: A Modern Introduction, 2nd Edition, Brooks/Cole, 2005.
3. B.S. Grewal, Higher Engineering Mathematics, Khanna Publishers, 36th Edition, 2010.

## Other useful resource(s):

1. Link to NPTEL course contents: https://onlinecourses.nptel.ac.in/noc18_ma05/preview
2. Link to topics related to course:
i. https://www.whitman.edu/mathematics/calculus_online/chapter14.html
ii. https://nptel.ac.in/courses/103103037/5
iii. https://nptel.ac.in/courses/111106051
iv. https://nptel.ac.in/courses/111107108/25
v. https://nptel.ac.in/courses/117101056/16

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (1) - 5 <br> Quizzes (2) - 15 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes (Engineering Mathematics I ) | B | ָ̛̀ | O | O | io | Oi | ì | $\stackrel{\infty}{\circ}$ | $\hat{i}$ | $\stackrel{\theta}{i}$ | $\begin{aligned} & 7 \\ & 0 \end{aligned}$ | OT | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 1 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 1 |
| CO-2 | 3 | 2 | 3 | 1 | 2 | 1 | 0 | 0 | 0 | 1 | 2 | 2 | 1.5 |
| CO-3 | 2 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 1 |
| CO-4 | 3 | 1 | 1 | 1 | 2 | 2 | 0 | 0 | 0 | 2 | 1 | 2 | 1.5 |
| CO-5 | 2 | 2 | 1 | 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 3 | 1.5 |
| CO-6 | 3 | 2 | 1 | 1 | 1 | 2 | 0 | 0 | 0 | 2 | 2 | 3 | 1.5 |
| Average | 2.67 | 1.5 | 1.17 | 1 | 1.5 | 1.5 | 0 | 0 | 0 | 1.67 | 1.5 | 2.17 |  |

## Basic Mathematics-I

COURSE CODE: 18B11MA112
COURSE CREDITS: 04
CORE/ELECTIVE: CORE
L-T-P: 3-1-0
Pre-requisite: Basic knowledge of Arithmetic and Algebra.

## Course Objectives:

1. To learn the basic concepts of Matrices and Determinant used in solving the system of linear equations.
2. To learn the fundamentals of vector, coordinate geometry and Complex number.
3. To learn and use the basic concepts of Differential and Integral Calculus

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Understand the basic properties of Matrices and Determinant, <br> Solution of system of linear equations |  <br> Usages |
| CO-2 | Understand the various concept of vectors and coordinate geometry | Familiarity |
| CO-3 | Understand complex numbers and their properties; geometrical <br> representation, Polar form. DeMoivre's theorem. Roots of complex <br> numbers | Familiarity |
| CO-4 | Work with sets, relations and functions |  |
| CO-5 | Understand the basic concept of Differential Calculus; limit <br> and continuity. Derivative. Rules of differentiation. Tangent <br> to a curve. Taylor's series. Maxima and minima. |  <br> Assessment |
| CO-6 | Understand the basic concept of Integral Calculus; Integrals <br> of elementary functions. Substitution and partial fractions. <br> Definite integral as a limit of sum. Properties of definite <br> integrals. Application to areas and lengths. | Assessment |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Matrices and Determinants Algebra of matrices. Determinant of a <br> square matrix. Properties of determinants. Some simple type of <br> matrices. Inverse of a matrix. Solution of equations | $\mathbf{8}$ |


| $\mathbf{2}$ | Vectors and Coordinate Geometry Vectors and their algebra. Unit <br> vectors. Components of a vector. Position vector. Direction cosines and <br> direction ratios. Dot and cross products. Projection of a vector on <br> another. Distance between two points. Equations of a line, plane and <br> sphere. Intersections. Shortest distance between lines and planes. | $\mathbf{9}$ |
| :---: | :--- | :---: |
| $\mathbf{3}$ | Complex Numbers Definition and geometrical representation. Algebra. <br> Complex conjugate. Modulus and amplitude. Polar form. DeMoivre's <br> theorem. Roots of complex numbers. Simple functions. | $\mathbf{6}$ |
| $\mathbf{4}$ | Sets, Relations and function Sets and their representation. Union, <br> intersection and compliment. Mapping or function. One-one, onto <br> mappings. Inverse and composite mappings. | $\mathbf{6}$ |
| $\mathbf{5}$ | Differential Calculus Basic concept of limit and continuity. <br> Derivative. Rules of differentiation. Tangent to a curve. Taylor's <br> series. Maxima and minima. | $\mathbf{6}$ |
| $\mathbf{6}$ | Integral Calculus Fundamental theorem of calculus (statement only). <br> Integrals of elementary functions. Substitution and partial fractions. <br> Definite integral as a limit of sum. Properties of definite integrals. <br> Application to areas and lengths. | $\mathbf{7}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. NCERT. Mathematics Textbook for class XI and XII.
2. R.D. Sharma, Mathematics, Dhanpat Rai Publications, New Delhi.

## Suggested Reference Book(s):

1. G. B Thomas, R. L. Finney Calculus and analytical geometry, 9th Ed., Pearson Education Asia (Adisson Wesley), New Delhi, 2000.
2. Erwin Kreyszig, Advanced Engineering Mathematics, 9th Edition, John Wiley \& Sons, 2006.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/122104018/
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111106086/2
ii. https://nptel.ac.in/courses/112104035/14
iii. https://nptel.ac.in/courses/111103070/
iv. https://nptel.ac.in/courses/111104085/8
v. https://nptel.ac.in/courses/111104085/14

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (1) - 5 <br> Quizzes (2) - 15 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes (Biostatistics ) | B | $\begin{aligned} & \text { No } \\ & \dot{O} \end{aligned}$ | $\hat{0}$ | I | $\begin{aligned} & \text { n } \\ & 0 \\ & \hline 0 \end{aligned}$ | Q | O | $\stackrel{\infty}{0}$ | $\hat{i}$ |  | $\begin{aligned} & 7 \\ & 0 \\ & 0 \end{aligned}$ | $\stackrel{\text { O}}{0}$ | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 2 | 2 | 2 | 3 | 3 | 2 | 1 | 3 | 2 | 3 | 3 | 24 |
| CO-2 | 3 | 1 | 1 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 1 | 2 | 18 |
| CO-3 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 1.2 |
| CO-4 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 3 | 1 | 2 | 13 |
| CO-5 | 3 | 2 | 2 | 3 | 2 | 2 | 2 | 1 | 2 | 1 | 3 | 2 | 2.1 |
| CO-6 | 3 | 3 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 1 | 2 | 2 | 2.0 |
| Average | 2.7 | 1.7 | 1.5 | 1.8 | 1.8 | 1.8 | 1.7 | 1.0 | 1.8 | 1.7 | 1.8 | 2.2 |  |

## Engineering Mathematics II

COURSE CODE: 18B11MA211
COURSE CREDITS: 4
CORE/ELECTIVE: CORE

## L-T-P: 3-1-0

## Pre-requisite: Engineering Mathematics I

## Course Objectives:

1. The various methods of solving the second order differential equations with variable coefficients, to study the basic properties of Bessel Functions, Legendre polynomials, Chebyshev polynomials and their Applications.
2. To obtain solutions of Wave, Diffusion and Laplace Equation.
3. To study calculus of complex variables.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Solve problems related to convergence of series |  <br> Usage |
| CO-2 | Understand basics of Ordinary Differential equation | Assessment |
| CO-3 | Comprehend series solution with certain special functions e.g. Bessel, <br> Legendre Eqn. | Usage |
| CO-4 | understand partial differential Eqn and Solve Heat, wave \& Laplace | Usage |
| CO-5 | Understand Functions of a complex variable, Analytic functions, <br> Mobius Transformation | Usage |
| CO-6 | Solve Contour integration and find Taylor's and Laurent's series |  |
| Usage |  |  |
| CO-7 | Evaluate certain real defnite and improper integrals. <br> Usage |  |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Sequences and Series: Convergence of sequence and series, tests for <br> convergence; Power series, Fourier series: Half range sine and cosine <br> series, Parseval's theorem. | $\mathbf{7}$ |


| $\mathbf{2}$ | Differential Equations Part I: Basics of first order Differential <br> Equations, Second and Higher order differential equations with constant <br> coefficients. Second order linear differential equations with variable <br> coefficients, method of variation of parameters, Cauchy-Euler equation; | $\mathbf{7}$ |
| :---: | :--- | :---: |
| $\mathbf{3}$ | Differential Equations Part II: Power series solutions; Legendre <br> polynomials, Bessel functions of the first kind and their properties. <br> Introduction to Partial Differential Equations, Solutions of One <br> dimensional Wave, Heat Equation \& Laplace Equation. | $\mathbf{1 2}$ |
| $\mathbf{4}$ | Complex Variable - Differentiation: Differentiation, Cauchy-Riemann <br> equations, analytic functions, harmonic functions, finding harmonic <br> conjugate; elementary analytic functions (exponential, trigonometric, <br> logarithm) and their properties; Conformal mappings, Mobius <br> transformations and their properties. | $\mathbf{8}$ |
| $\mathbf{5}$ | Complex Variable - Integration: Contour integrals, Cauchy Theorem, <br> Cauchy Integral formula, Liouville's theorem and Maximum-Modulus <br> theorem; Taylor's series, zeros of analytic functions, singularities, <br> Laurent's series; [CO-6] Residues, Cauchy Residue theorem, Evaluation <br> of definite integral involving sine and cosine, improper integrals. | $\mathbf{8}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. Erwin Kreyszig, Advanced Engineering Mathematics, 9th Edition, John Wiley \& Sons, 2006
2. Jain and Iyengar, Advanced Engineering Mathematics, Narosa Publishing House

## Suggested Reference Book(s):

1. Simmons, G.F., Differential Equations with Applications, 2nd Ed, McGraw-Hill, 1991.
2. Brown, J.W., Churchill, R.V., Complex Variables and Applications, 6th Ed., McGrawHill, 1996.
3. Spiegel, Murray R, Theory and Problems of Complex variables Schaum's series.
4. Sneddon I. N., Introduction to Partial Differential Equations, Dover Publications, 2006

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/122101003/2
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111104031/
ii. https://nptel.ac.in/courses/111104031/8
iii. https://nptel.ac.in/courses/122107037/29
iv. https://nptel.ac.in/courses/111107056/
v. https://nptel.ac.in/courses/117101055/14

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semeste <br> r | Assignment (1) - 5 <br> Quizzes (2) - 15 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes <br> (Engineering <br> Mathematics II ) | B | ố | $0$ | jo | in | Ò | $\hat{o}$ | $\stackrel{\infty}{i}$ | $\hat{i}$ | $\stackrel{0}{0}$ | $\underset{B}{7}$ | ה̃ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 1 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 1 |
| CO-2 | 2 | 2 | 1 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 1.5 |
| CO-3 | 3 | 2 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 1 | 1 | 3 | 1.5 |
| CO-4 | 3 | 1 | 2 | 1 | 2 | 2 | 0 | 0 | 0 | 2 | 1 | 2 | 1.5 |
| CO-5 | 2 | 2 | 1 | 2 | 1 | 1 | 0 | 0 | 0 | 2 | 2 | 2 | 1.5 |
| CO-6 | 3 | 2 | 2 | 1 | 2 | 1 | 0 | 0 | 0 | 1 | 2 | 1 | 1.5 |
| CO-7 | 3 | 1 | 1 | 0 | 2 | 2 | 0 | 0 | 0 | 2 | 1 | 2 | 1.5 |
| Average | 2.71 | 1.57 | 1.14 | 1 | 1.71 | 1.42 | 0 | 0 | 0 | 1.57 | 1.42 | 1.85 |  |

## Basic Mathematics II

COURSE CODE: 18B11MA212
COURSE CREDITS: 04
CORE/ELECTIVE: CORE
L-T-P: 3-1-0

## Pre-requisite: Basic Mathematics-I (18B11MA112)

## Course Objectives:

1. To acquire the basic knowledge of sequence, series and advanced calculus.
2. To study the differential equations and their solutions applicable in Biotechnology and Bioinformatics.
3. To study the fundamentals and applications of Statistics and Numerical Techniques used in Bio sciences.

Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Understand the idea of sequence and series and to learn about their <br> convergence | Familiarity |
| CO-2 | learn concepts of calculus of two or more variables | Familiarity |
| CO-3 | learn the fundamentals of differential equations and their types | Familiarity |
| CO-4 | Solve various types of differential equations | Assessment |
| CO-5 | Understand basic statistics and learn to find mean mode, <br> median and standard deviation. | Usage |
| CO-6 | Numerically solve various problems using standard methods | Usage |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Sequence and series: Convergence and divergence. Simple tests for <br> convergence. Absolute convergence. | $\mathbf{8}$ |
| $\mathbf{2}$ | Calculus of two or more variables: Partial differentiation. Taylor's <br> series. Differentiation of a vector. Tangent to a curve. Gradient of a <br> scalar. Tangent to a surface. Integration of a vector. Line integral. <br> Double integral. | $\mathbf{8}$ |


| $\mathbf{3}$ | Elementary Differential Equations: Definitions of order, degree, <br> linear, nonlinear, homogeneous and nonhomogeneous Solution of first <br> order equations. Complementary function and particular integral. Initial <br> and boundary value problems. Linear differential equations with <br> constant coefficients. Cauchy-Euler equation | $\mathbf{1 0}$ |
| :---: | :--- | :---: |
| $\mathbf{4}$ | Basic Statistics: Classification of data. Mean, mode, median and <br> standard deviation. Method of least squares | $\mathbf{8}$ |
| $\mathbf{5}$ | Numerical Methods: Newton-Raphson method. Linear and quadratic <br> interpolation. Simpson's rule | $\mathbf{8}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. G. B Thomas, R. L. Finney Calculus and analytical geometry, $9^{\text {th }}$ Ed., Pearson Education Asia (Adisson Wesley), New Delhi, 2000.
2. NCERT. Mathematics Textbook for class XI and XII.
3. Sharma, R.D. Mathematics, Dhanpat Rai Publications, New Delhi

## Suggested Reference Book(s):

1. Erwin Kreyszig, Advanced Engineering Mathematics, 9th Edition, John Wiley \& Sons, 2006
2. Dennis G. Zill, Warren S. Wright, Advanced Engineering Mathematics, Jones and Bartlett Publishers, Inc; 4th Revised edition.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111104085/25
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111108081/
ii. https://nptel.ac.in/courses/105103027/module2/lec5/1.html
iii. https://www.khanacademy.org/math/ap-statistics/summarizing-quantitative-data-ap/measuring-center-quantitative/v/statistics-intro-mean-median-and-mode

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |


| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (2)-5 <br> Quizzes (2) - 15 |
| :---: | :--- | :--- | :--- | :--- |
|  |  |  | Attendance - 5 |  |

Course Outcomes (COs) contribution to the Programme Outcomes(POs)

| Course outcomes <br> (Parallel and <br> Distributed <br> Algorithms ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

## Numerical Methods

## COURSE CODE: 18B11MA311

COURSE CREDITS:4
CORE/ELECTIVE: CORE
L-T-P: 3-1-0

## Pre-requisite: None

## Course Objectives:

1. Introduction to numerical errors and various techniques for obtaining roots of the nonlinear equations.
2. Learn to analyze system of linear equations and obtain its solutions.
3. To learn certain interpolation techniques.
4. To comprehend numerical differentiation and integration.
5. Learn to obtain solutions of IVP, BVP and partial differential equations.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | To understand numerical errors and obtain roots of the nonlinear <br> equations \& system of nonlinear equations. | Assessment |
| CO-2 | Ability to solve the system of linear equations and finding <br> eigenvalues of the matrices. | Assessment |
| CO-3 | Perform polynomial interpolations using various techniques. | Usage |
| CO-4 | Perform Cubic-spline interpolation and approximations. | Assessment |
| CO-5 | Perform Numerical Differentiation, Numerical Integration. | Assessment |
| CO-6 | Solve IVP, BVP and numerical solutions of parabolic, elliptic <br> and hyperbolic partial differential equations. | Assessment |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Introduction to numerical errors and nonlinear equations: Initial <br> error, round-off error, Truncation error, Absolute error, relative error, <br> percentage error. Root-finding methods: single nonlinear equation <br> Bisection method, False-Position method, Newton-Raphson method, <br> Secant methods, (Fixed-point) Iteration method; more than one <br> nonlinear equations- Newton's method. Convergence criteria. Iterative <br> methods and the formula for calculation of the approximation. | $\mathbf{6}$ |


| $\mathbf{2}$ | Numerical Linear Algebra: Direct methods: Gauss-elimination <br> method, LU-Decomposition methods. Iterative methods: Gauss-Siedel <br> method, Successive Over-Relaxation (SOR) methods. Eigenvalue <br> problem: Power method for largest eigenvalue, Jacobi's method for <br> symmetric matrices. | $\mathbf{6}$ |
| :---: | :--- | :---: | :---: |
| $\mathbf{3}$ | Interpolation \& Approximation: (i) Interpolating polynomial. Lagrange <br> formula with error. Formulae for equally-spaced points. Divided <br> differences: Newton's interpolating polynomials. <br> (ii) Hermite interpolation. Cubic-spline interpolation. Pade and rational <br> approximations. Least square approximation. Approximation by splines. | $\mathbf{5 + 5 = 1 0}$ |
| $\mathbf{4}$ | Numerical Differentiation and Quadrature: Approximation of <br> derivatives, Newton-cote integration formulae. Gauss-Legendre <br> quadrature formulae. Romberg integration. Double integration. | $\mathbf{9}$ |
| $\mathbf{5}$ | Numerical Solutions of ODE and PDE: Numerical solutions of <br> ODEs using Picard, Euler, modified Euler, Runge-Kutta methods, <br> Predictor corrector methods for IVPs. The Finite difference method <br> and Shooting method for BVPs. Numerical solutions of parabolic, <br> elliptic and hyperbolic partial differential equations. | $\mathbf{1 1}$ |
| $\mathbf{T o t a l}$ lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. C. F. Gerald and P.O Wheatley: Applied Numerical Analysis, $6^{\text {th }}$ Edition, Pearson Education Asia, New Delhi, 2002.
2. Steven C. Chapra, Raymond P. Canale: Numerical Methods for Engineers, $7^{\text {th }}$ Edition, Tata McGraw-Hill.
3. M. K. Jain, S.R.K. Iyengar, R. K. Jain: Numerical Methods for Scientific and Engineering Computation, $6^{\text {th }}$ Edition, New Age International.

## Suggested Reference Book(s):

1. S. Joe D Hoffman: Numerical Methods for Engineers and Scientists, $2^{\text {nd }}$ Edition, Marcel Dekker Inc.
2. Richard L. Burden \& J. Douglas Faires: Numerical Analysis, $9^{\text {th }}$ Edition, Cengage Learning.
3. B. S. Grewal: Numerical Methods, $11^{\text {th }}$ Edition, Khanna Publishers.
4. S. S. Sastry: Introductory Methods of Numerical Analysis, $5{ }^{\text {th }}$ Edition, Prentice Hall India Learning Private Limited.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/122102009/

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (2) - 15 <br> Quizzes (1) -5 <br> Attendance -5 |

## Course Outcomes (COs) contribution to the Programme Outcomes(POs)

| Course outcomes <br> (Numerical <br> Methods) | B | Ò | $\hat{0}$ | E | $\begin{aligned} & \text { n } \\ & 0 \\ & \hline 1 \end{aligned}$ | Oí | $\hat{i}$ | $\stackrel{\infty}{i}$ | $\hat{\hat{i}}$ | $\stackrel{e}{i}$ | $\begin{aligned} & 7 \\ & 0 \end{aligned}$ | T |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 2 | 3 | 2 | 2 | 2 | 1 | 0 | 0 | 1 | 2 | 2 | 2 | 1.6 |
| CO-2 | 2 | 2 | 1 | 2 | 3 | 3 | 0 | 0 | 1 | 2 | 2 | 2 | 1.7 |
| CO-3 | 1 | 1 | 2 | 2 | 2 | 2 | 0 | 0 | 2 | 2 | 2 | 2 | 1.5 |
| CO-4 | 2 | 2 | 2 | 2 | 1 | 2 | 0 | 0 | 2 | 1 | 1 | 2 | 1.4 |
| CO-5 | 3 | 2 | 2 | 2 | 2 | 2 | 0 | 0 | 2 | 2 | 2 | 2 | 1.8 |
| CO-6 | 2 | 2 | 1 | 2 | 2 | 2 | 0 | 0 | 2 | 1 | 1 | 1 | 1.3 |
| Average | 2 | 2 | 1.7 | 2 | 2 | 2 | 0 | 0 | 1.7 | 1.7 | 1.7 | 1.8 |  |

## Probability and Statistical Techniques

COURSE CODE: 18B11MA312

## COURSE CREDITS: 4

CORE/ELECTIVE: CORE

## L-T-P: 3-1-0

## Pre-requisite: Working knowledge of basic calculus and combinatorial skills.

Course Objectives: This course introduces students:

1. To the elementary concepts of descriptive and inferential techniques of statistical methodology.
2. To extend and formalize knowledge of the theory of probability and random variables.

Course Outcomes: At the end of the course, the students will be able to apply appropriate statistical concepts, methodologies and technologies in organizing, analyzing and interpreting various real-world situations and in coming up with relevant decisions:

| S. No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Compute and Interpret Measures of Central Tendency and <br> Dispersion of Data; Construct and Analyze Graphical Displays <br> (Histogram, Bar \& Pie Charts, Etc.) To Summarize Data. | Familiarity |
| CO-2 | Construct Sample Spaces of Random Experiments; Identify and <br> Specify Events; Apply Discrete/Continuous Probability <br> Distributions to Evaluate Event Probabilities; Use Central Limit <br> Theorem to Find Probabilities for Sampling Distributions. | Assessment |
| CO-3 | Conduct Hypotheses Tests \& Construct Point \& Confidence-Interval <br> Estimates Concerning Population Parameters Based on Sample <br> Data; Perform and Interpret Chi-Square Test of Goodness-of-Fit and <br> Test of Independence. | Usage |
| CO-4 | Compute Correlation Coefficient to Decide The Linear <br> Relationship that May Exist Between Two Variables of <br> Interest; Find The Equation of Regression Line And Predict <br> The Value of One Variable Based on the Value of the Other <br> Variable. | Assessment |
| CO-5 | Identify and Evaluate Common Sampling Techniques Such as <br> F-Test in ANOVA - Evaluating or Approximating the P- <br> Value of the Test Statistic - and Design Simple Experimental. | Applications |

## Course Contents:

| Unit | Contents | Lectures <br> Required |
| :---: | :---: | :---: |


| $\mathbf{1}$ | Basics of Statistics: Population, Sample, Attribute and Variable (Discrete <br> and Continuous). Classification and Tabulation of Data. Graphical <br> Representation of Data - Histogram, Frequency Polygon, Stem-and-Leaf <br> Plots, Box Plot, Bar \& Pie Charts. [CO-1] | $\mathbf{5}$ |
| :---: | :--- | :---: |
| $\mathbf{2}$ | Descriptive statistics: Measures of Central Tendency - Mean, Median, <br> Mode. <br> Dispersion and its Measures - Range, Quartile Deviation, Mean <br> Deviation, Standard Deviation. Skewness and Kurtosis. [CO-1] | $\mathbf{6}$ |
| $\mathbf{3}$ | Probability: Random Experiment, Sample Space, Event, Types of Events. <br> Three Approaches To Probability, Additive And Multiplicative Laws, Of <br> Probability, Conditional Probability, Total Probability Theorem and Bayes <br> Theorem. [CO-2] | $\mathbf{5}$ |
| $\mathbf{4}$ | Random Variables: Random Variable - Introduction: Probability Mass <br> Function (PMF), Probability Density Function (PDF) and Cumulative <br> Distribution Function (CDF). Moments of Random a Variable - Mean and <br> Variance. Moment Generating Function of a Random Variable (Definition <br> \& Properties). Bernoulli, Binomial, Poisson and Normal Distributions <br> Problems with Applications. [CO-2] | $\mathbf{6}$ |
| $\mathbf{5}$ | Statistical Inference: Introduction to Random Sampling - The Central <br> Limit Theorem, Sampling Distribution. Concept of Estimation and Testing <br> of Hypotheses: Type-I \& Type-II Errors, Level of Significance, <br> Confidence Interval, P-Value, Critical Value, Critical Region; Tests for <br> Population Means and Variances for Single and Double Samples (Z-Test, <br> T-Test and F-Test). Chi-Square Test of Goodness of Fit and Independence <br> of Attributes (mxn Contingency). [CO-3] | $\mathbf{8}$ |
| $\mathbf{6}$ | Correlation And Regression: Bivariate Data, Scatter Plots. Pearson <br> Product-Moment and Spearman's Rank Correlation Coefficients, Properties <br> of Correlation Coefficient. <br> Simple Linear Regression - Regression Equations. [CO-4] | $\mathbf{6}$ |
| $\mathbf{7 0 t a l}$ Lectures | ANOVA and Simple Designs: One-Way and Two-Way (Without and <br> With Interaction) ANOVA. Concept of Three Basic Principles of Design <br> of Experiments, CRD and RBD. [CO-5] | $\mathbf{6}$ |

## Suggested Text Book(s):

1. Richard A. Johnson Irwin Miller and John E. Freund, ‘`Probability and Statistics for Engineers", Prentice Hall, New Delhi, $11^{\text {th }}$ Edition, 2011.

## Suggested Reference Book(s):

1. Ronald E. Walpole , Raymond H. Myers , Sharon L. Myers and Keying E. Ye, '"Probability and statistics
for engineers and scientists", $9^{\text {th }}$ Edition, Pearson, 2011.
2. Jay L. Devore, "Probability and statistics for engineering and the sciences", Cengage Learning, 8th Edition, 2011.
3. P. Kousalya, "Probability, statistics and random processes", Pearson Education, 2013.

## Other Useful Resource(s):

1. Link to NPTEL Course Contents:
i. https://nptel.ac.in/courses/111106112/
ii. https://nptel.ac.in/courses/111105090/
iii. https://nptel.ac.in/courses/111105041/
iv. https://nptel.ac.in/courses/102106051/
v. https://nptel.ac.in/courses/102101056/
2. Link to Topics Related to Course:
i. https://nptel.ac.in/courses/111106112/1-5/
ii. https://nptel.ac.in/courses/111106112/12-17/
iii. https://nptel.ac.in/courses/111106112/18-21/
iv. https://nptel.ac.in/courses/111105090/1-32/
v. https://nptel.ac.in/courses/111105090/49-54/
vi. https://nptel.ac.in/courses/111105090/61-79/
vii. https://nptel.ac.in/courses/111105041/3-40/
viii. https://nptel.ac.in/courses/102106051/32/
ix. https://nptel.ac.in/courses/102106051/1-24/
x. https://nptel.ac.in/courses/102101056/1-12/
xi. https://nptel.ac.in/courses/102101056/15-40/

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage /Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (2) - 10 <br> Quizzes (2) - 10 <br> Attendance - 5 |

Course Outcomes (COs) Contribution to the Programme Outcomes (POs):

| Course Outcomes (Probability \& Statistics) | Ò | Ǹ | $2$ | + | $\begin{aligned} & \text { in } \\ & \dot{O} \end{aligned}$ | Oí | ì | か | $\hat{i}$ | $0$ | $7$ | I | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 3 | 1 | 2 | 1 | 1 | 1 | - | - | 1 | 2 | 1 | 1.6 |
| CO-2 | 3 | 3 | 1 | 2 | 2 | 1 | 1 | - | - | 1 | 2 | 2 | 1.8 |
| CO-3 | 3 | 3 | 2 | 3 | 3 | 3 | 1 | - | - | 1 | 3 | 3 | 2.5 |
| CO-4 | 3 | 3 | 3 | 3 | 2 | 3 | 1 | - | - | 2 | 3 | 3 | 2.7 |
| CO-5 | 3 | 3 | 3 | 3 | 3 | 3 | 1 | - | - | 2 | 3 | 3 | 2.7 |
| Average | 3.0 | 3.0 | 2.0 | 2.6 | 2.4 | 2.2 | 1.0 | - | - | 1.4 | 2.6 | 2.4 |  |

## Probability and Statistics

COURSE CODE: 18B11MA313
COURSE CREDITS: 4
CORE/ELECTIVE : CORE
L-T-P: 3-1-0

Pre-requisite: Working knowledge of basic calculus from Engineering Mathematics-I (18B11MA111).

## Course Objectives:

1. To introduce students, the theoretical knowledge of the probability of random variables.
2. To study the fundamental concepts of descriptive and inferential techniques of statistical methodology.

## Course Outcomes:

| S. No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Construct sample spaces of random experiments; identify and specify <br> events, and perform set operations on events; understand the <br> axiomatic approach of probability theory; compute probabilities by <br> counting; evaluate conditional probability, and apply Bayes' theorem <br> to simple situations. |  <br> Assessment |
| CO-2 | Express random variables by using distribution function and density <br> functions; calculate moments related to random variables; understand <br> the concept of inequalities and probabilistic limits; understand the <br> intrinsic need of (functions of) random variables for the analysis of <br> random phenomena. |  <br> Assessment |
| CO-3 | Compute probability distributions and correlation measures of <br> bivariate random variables; obtain marginal and conditional <br> distributions of random variables; find probabilities for outcomes of <br> various events related to an uncertain phenomenon using appropriate <br> probability distributions as models. |  <br> Usage |
| CO-4 | Compute correlation coefficient to decide the linear relationship that <br> may exist between two variables of interest; find the equation of <br> regression line and second degree curve, and to predict the value of <br> one variable based on the value of the other variable. |  <br> Assessment |
| CO-5 | Use central limit theorem to find probabilities for sampling <br> distributions; conduct hypotheses tests and construct confidence-- <br> interval estimates concerning population parameters based on sample <br> data; perform and interpret chi-square test of goodness-of-fit and test <br> of independence. |  <br> Usage |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Basic probability: Random experiments; three basic approaches to <br> probability, combinatorial probability problems; conditional probability, <br> independence; total probability theorem, Bayes' theorem. | $\mathbf{4}$ |
| $\mathbf{2}$ | Random variables: Concept of random variables - discrete, continuous; <br> probability distributions - probability mass function, density function and <br> cumulative distribution function; expectation, variance and moment <br> generating function of random variables; Chebyshev's inequality; <br> bivariate distributions - conditional densities, distribution of sums and <br> quotients, covariance (definition and interpretation). | $\mathbf{1 0}$ |
| $\mathbf{3}$ | Probability distributions: Binomial, multinomial and Poisson <br> approximation to the binomial distribution; exponential, gamma, and <br> normal distributions. | $\mathbf{6}$ |
| $\mathbf{4}$ | Descriptive statistics: Measures of central tendency \& dispersion: <br> evaluation of statistical parameters (mean and variance possibly from <br> grouped data) for binomial, Poisson and normal distributions; Measures <br> of skewness and kurtosis; correlation and regression - rank correlation <br> and curve fitting of straight lines, second degree parabolas and more <br> general curves. | $\mathbf{1 0}$ |
| $\mathbf{5}$ | Inferential statistics: Introduction to sampling distribution - central <br> limit theorem; testing of hypotheses: critical value, critical region, <br> confidence interval, level of significance, p-value; Large and small <br> sample tests (Z-test, t-test and F-test): single proportion, difference of <br> proportions, single mean, difference of means, difference of standard <br> deviations, and tests for ratio of variances and correlation coefficients; <br> Chi-square test of goodness-of-fit and independence of attributes. | $\mathbf{1 2}$ |
| Total Lectures |  |  |

## Suggested Text Book(s):

1. Richard A. Johnson Irwin Miller and John E. Freund, `Probability and Statistics for Engineers", Prentice Hall, New Delhi, 11th Edition, 2011.
2. Jay L. Devore, "Probability and statistics for engineering and the sciences", Cengage Learning, 8th Edition, 2011.

## Suggested Reference Book(s):

1. Ronald E. Walpole, Raymond H. Myers, Sharon L. Myers and Keying E. Ye, `Probability and statistics for engineers and scientists'", $9^{\text {th }}$ Edition, Pearson, 2011.
2. Henry Stark and John W. Woods: "Probability and random processes with applications to signal processing', Pearson education, $3^{\text {rd }}$ Edition, Asia, 2002.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111106112
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111105090/
ii. https://nptel.ac.in/courses/111101004/
iii. https://nptel.ac.in/courses/111102111/

## Evaluation Scheme:

| S. No. | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1.0 Hour | Syllabus covered up to T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered up to T-2 |
| 3. | T-3 | 35 | 2.0 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semeste <br> r | Assignment (1) - 05 <br> Quizzes (2) - 15 <br> Attendance |

## Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course Outcomes (Probability \& Statistics) | ì | Ǹ | $0$ | + | ®i | Oi | $\hat{i}$ | $\stackrel{\infty}{i}$ | $\hat{i}$ | $\stackrel{\theta}{i}$ | $7$ | $\frac{7}{1}$ | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 3 | 1 | 2 | 1 | 1 | 1 | - | - | 1 | 2 | 1 | 1.6 |
| CO-2 | 3 | 3 | 1 | 2 | 2 | 1 | 1 | - | - | 1 | 2 | 2 | 1.8 |
| CO-3 | 3 | 3 | 2 | 3 | 3 | 3 | 1 | - | - | 1 | 3 | 3 | 2.5 |
| CO-4 | 3 | 3 | 3 | 3 | 2 | 3 | 1 | - | - | 2 | 3 | 3 | 2.7 |
| CO-5 | 3 | 3 | 3 | 3 | 3 | 3 | 1 | - | - | 2 | 3 | 3 | 2.7 |
| Average | 3.0 | 3.0 | 2.0 | 2.6 | 2.4 | 2.2 | 1.0 | - | - | 1.4 | 2.6 | 2.4 |  |

## Probability Theory and Random Processes

## COURSE CODE: 18B11MA314

## COURSE CREDITS: 4

## CORE/ELECTIVE: CORE

## L-T-P : 3-1-0

## Pre-requisite: Knowledge of Differential \& Integral Calculus from Engineering Mathematics-I.

## Course Objectives:

1. To provide the students the elementary concepts of descriptive and inferential statistical methods.
2. To extend and familiarize the students with the basic concepts of random process for applications such as Random signals, signal noise, linear systems, etc in communication engineering.

## Course Outcomes:

| S. No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Construct sample spaces of random experiments; identify and specify <br> events, and perform set operations on events; compute probabilities by <br> counting; evaluate conditional probability, and apply Bayes' theorem <br> to simple situations. |  <br> Usage |
| CO-2 | Express random variables by using CDFs, PMFs; calculate <br> moments related to random variables; understand the concept of <br> inequalities and probabilistic limits. Understand the axiomatic <br> approach of probability theory and intrinsic need of (functions of |  <br> Assessment |
| CO-3 | Compute probability distributions and correlation measures of <br> bivariate random variables; obtain marginal and conditional <br> distributions of random variables; find probabilities for outcomes of <br> various events related to an uncertain phenomenon using appropriate <br> probability distributions as models. |  <br> Usage |
| CO-4 | Conduct hypotheses tests concerning population parameters based on <br> sample data; perform and interpret chi-square test of goodness-of-fit <br> and test of independence; find the equation of regression line and <br> second degree curve, and to predict the value of one variable based on <br> the value of the other variable. |  <br> Usage |
| CO-5 | Identify and classify random processes and determine covariance and <br> spectral density of stationary and ergodic random processes; <br> demonstrate specific applications to Gaussian process. |  <br> Usage |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Basic probability: Random experiments; Three basic approaches to <br> probability, combinatorial probability problems; Conditional probability, <br> total probability theorem, Bayes' theorem. | $\mathbf{4 L}$ |
| $\mathbf{2}$ | Random variables: Univariate random variables - discrete, continuous <br> and mixed random variables; probability distributions - probability mass <br> function, density function and cumulative distribution function; | 10L |
|  | Expectation, variance and moment generating function of random <br> variables; Chebyshev's inequality; Bivariate distributions with properties <br> conditional densities, definition \& interpretation of covariance with <br> properties, distributions of sum and quotient of random variables. |  |
| $\mathbf{3}$ | Special distributions: Bernoulli trials - binomial, multinomial and <br> Poisson distributions; Exponential, gamma, uniform, and Gaussian <br> distributions. | $\mathbf{6 L}$ |
| $\mathbf{4}$ | Basic statistics: Measures of central tendency \& dispersion: evaluation <br> of statistical parameters (mean and variance possibly from grouped data) <br> for binomial and normal distributions; Measures of skewness and <br> kurtosis; Correlation and regression - rank correlation and curve fitting <br> by the method of least squares regression - fitting of straight lines, second <br> degree parabolas. | $\mathbf{6 L}$ |
| $\mathbf{5}$ | Applied statistics: Introduction to sampling distribution; Testing of <br> hypotheses: critical value, critical region, confidence interval, level of <br> significance, p-value; Test for one sample proportion \& Tests for mean <br> and variance for single and double samples: Z-test, t-test and F-test; <br> Chi-square test of goodness-of-fit and independence of attributes. | $\mathbf{1 0 L}$ |
| $\mathbf{l}$Stochastic processes: Introduction and classification of random <br> processes; Statistical averages - mean and auto-correlation functions; <br> Stationary processes - SSS and WSS processes; Ergodic processes, <br> Gaussian process - covariance matrix; Linear system with random inputs, <br> power spectral density, noise in communication systems, white Gaussian <br> noise. | $\mathbf{6 L}$ |  |
| $\mathbf{T o t a l}$ Lectures | $\mathbf{4 2 L}$ |  |

## Suggested Text Book(s):

1. Richard A. Johnson Irwin Miller and John E. Freund, `’Probability and Statistics for Engineers", Prentice Hall, New Delhi, 11th Edition, 2011.
2. Oliver C. Ibe, `'Fundamentals of applied probability and random processes", Academic press, 2005.

## Suggested Reference Book(s):

1. Ronald E. Walpole, Raymond H. Myers, Sharon L. Myers and Keying E. Ye, `’Probability and statistics for engineers and scientists', 9th Edition, Pearson, 2011.
2. Jay L. Devore, '`Probability and statistics for engineering and the sciences", Cengage Learning, 8th Edition, 2011.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111102111
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111101004/2
ii. https://nptel.ac.in/courses/111106112/1
iii. https://nptel.ac.in/courses/117105085/30
iv. https://nptel.ac.in/courses/108103112/14

## Evaluation Scheme:

| S. No. | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1.0 Hours | Syllabus covered up to T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered up to T-2 |
| 3. | T-3 | 35 | 2.0 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (1) - 05 <br> Quizzes (2) -15 <br> Attendance -05 |

## Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course Outcomes [Probability Theory \& Random Processes] | O | Ò | ô | O | in | oi | 人̀ | $\stackrel{\infty}{0}$ | $\hat{i}$ | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | 7 | I | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 3 | 1 | 1 | 1 | 1 | 1 | - | - | 1 | 2 | 1 | 1.6 |
| CO-2 | 3 | 3 | 1 | 2 | 2 | 1 | 1 | - | - | 1 | 2 | 2 | 1.8 |
| CO-3 | 3 | 3 | 2 | 3 | 3 | 3 | 1 | - | - | 1 | 3 | 3 | 2.5 |
| CO-4 | 3 | 3 | 3 | 3 | 3 | 3 | 1 | - | - | 2 | 3 | 3 | 2.7 |
| CO-5 | 3 | 2 | 2 | 2 | 3 | 3 | 2 | - | - | 1 | 3 | 3 | 2.3 |
| Average | 3.0 | 2.8 | 1.8 | 2.4 | 2.4 | 2.0 | 1.2 | - | - | 1.2 | 2.6 | 2.4 |  |

## Discrete Mathematics

## COURSE CODE: XXXXXX

## COURSE CREDITS: 4

## CORE / ELECTIVE: CORE

L-T-P: 3-1-0
Pre-requisite: None

## Course Objectives:

1. To learn various discrete structures (e.g., sets, relations, logic, lattices, graphs, linear transformations, structure of language etc.) that provide the mathematical formalizations for computational problems.
2. Learn Mathematical arguments and proof techniques.
3. Study of certain algebraic structures.
4. To comprehend Languages, grammars, FSA and FSM.

## Course Outcomes:

| S. No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Understand set operations, various types of relations and their <br> representations, solving recurrence relations. | Familiarity |
| CO-2 | Comprehend the discrete structures of lattices, Propositions with proof <br> of validity of arguments and quantifiers. | Assessment |
| CO-3 | Understand various types of graphs, paths, spanning trees, planarity of <br> graphs and coloring theorems. | Usage |
| CO-4 | Recognize Algebraic structures; Groups, Subgroups, Rings, Fields with <br> extension to concepts of vector spaces, dimensions and linear <br> transformations. | Assessment |
| CO-5 | Comprehend Languages, grammars, finite state automata and finite state <br> machines. | Assessment |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :---: | :---: |
| $\mathbf{1}$ | Set, Relations and Functions: Basic operations on sets, Cartesian <br> products, disjoint union (sum), and power sets. Partitions and Duality. | $\mathbf{8}$ |


|  | Different types of relations, their compositions and inverses. Different <br> types of functions, Recursively defined functions, Recursive algorithms, <br> generating functions and solutions of recurrence relations, Complexity of <br> algorithms, Big-o notation, Euclidean algorithm for finding GCD, <br> Evaluation of polynomial using Horner's method, Russian Peasant <br> method for multiplication. |  |
| :---: | :--- | :---: |
| $\mathbf{2}$ | Lattices and Propositional Logic: Ordered Sets and Lattices: Partial <br> order relations and Hasse diagram, Supremum and infimum, total <br> ordering, lattices - bounded, distributive, complemented, modular, <br> Product of lattices. Simple and compound statement. logical operators. <br> Implication and double implication, Tautologies and contradictions. <br> Valid arguments and fallacy. Propositional functions and quantifiers. | $\mathbf{8}$ |
| $\mathbf{3}$ | Graph Theory: Graphs and their basic properties - degree, path, cycle, <br> subgraph, isomorphism, Eulerian and Hamiltonian walk, Matrix <br> representation of Graphs and properties, Planar Graphs, <br> Homeomorphism, Kuratowski's theorem, Spanning trees, shortest <br> spanning tree, Algorithms for finding shortest spanning tree Graph <br> colorings. Four color problem, Digraphs and related definitions, <br> connectivity in diagraphs. | $\mathbf{1 0}$ |
| $\mathbf{4}$ | Algebraic structures \& Vector Space: Binary operations, Algebraic <br> structures - semigroup, monoid, groups, subgroups, Rings, Integral <br> domain and fields, Vector Space, linear dependence of vectors, basis, <br> dimension; Linear transformations (maps), range and kernel of a linear <br> map, rank and nullity theorem. | $\mathbf{1 2}$ |
| $\mathbf{5}$ | Introduction to Languages: Introduction to Languages, finite state <br> automata grammars, finite state machines. | $\mathbf{4}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. Kenneth H. Rosen: Discrete Mathematics and Its Applications with combinatorics and Graph Theory, $7^{\text {th }}$ Edition, Tata McGraw-Hill, 2011.
2. Kolman B., Busby R., Ross S.: Discrete Mathematical Structures, $6^{\text {th }}$ Edition, Pearson Education, 2009.
3. Lipschutz S, Lipson M: Linear Algebra, $3^{\text {rd }}$ Edition, Schaum's outlines, Mc Graw-Hill International Edition, 2001.

## Suggested Reference Book(s):

1. Liu, C. L.: Elements of Discrete Mathematics, $3^{\text {rd }}$ Edition, Tata McGraw-Hill, 2008.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111107058/

## Evaluation Scheme:

| S. No. | Exam | Marks | Duration | Coverage/Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3 | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4 | Teaching Assessment | 25 | Entire <br> Semester | Quiz - 15 <br> Tutorial Quiz - 5 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the programme Outcomes (POs):

| Course outcomes <br> (Discrete Mathematics) | B | Ò | ô | O | eí | Oi | $\hat{o}$ | $\stackrel{\infty}{0}$ | $\hat{i}$ | e | B | I | 品 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 2 | 3 | 2 | 2 | 2 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1.3 |
| CO-2 | 2 | 2 | 2 | 2 | 2 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1.2 |
| CO-3 | 3 | 2 | 2 | 3 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1.3 |
| CO-4 | 3 | 2 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 0.8 |
| CO-5 | 3 | 2 | 3 | 2 | 3 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1.1 |
| Average | 2.6 | 2.2 | 2 | 2 | 1.8 | 1 | 0 | 0 | 1 | 1 | 1 | 1 |  |

## Biostatistics

COURSE CODE: 18B11MA421
COURSE CREDITS: 4
CORE/ELECTIVE: CORE
L-T-P: 3-1-0
Pre-requisite: Probability and Statistical Techniques.

## Course Objectives:

1. To study multiple linear regression and correlation model.
2. To study non-parametric tests, stochastic process and clustering along with their application in Bio-informatics.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Perform correlation and regression analysis and draw conclusions and <br> apply to Bio-informatics models. |  <br> Usage |
| CO-2 | Use method of least squares and evaluate least squares estimates. | Assessment |
| CO-3 | Execute non parametric tests and run tests and draw conclusions. | Usage |
| CO-4 | Understand stochastic processes and find ensemble averages, <br> mean function, auto - correlation and auto-covariance <br> functions, SSS and WSS processes. | Usage |
| CO-5 | Understand the Markov chains and apply Markov processes. | Usage |
| CO-6 | Apply clustering algorithms and its applications to large <br> databases and use clustering with categorical attributes. | Usage |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Regression and Correlation: Introduction - linear regression and <br> multiple regression (linear \& polynomial). Normal regression analysis <br> estimation of regression coefficients and confidence intervals. Normal <br> correlation analysis - method of maximum likelihood. Multiple linear <br> regression (method of least squares and matrix notation). | $\mathbf{8}$ |
| $\mathbf{2}$ | Method of Least Squares - normal equations and least squares <br> estimates. | $\mathbf{2}$ |


| $\mathbf{3}$ | Non-Parametric Tests: Need of non-parametric tests. Sign test for one <br> sample and two samples, signed-rank test, Wilcoxon test (Mann-Whitney <br> test), Run test for randomness. Distribution-free ANOVA: Kruskal- <br> Wallis and Friedman's test. | $\mathbf{9}$ |
| :---: | :--- | :---: |
| $\mathbf{4}$ | Stochastic Processes: Introduction and classification of stochastic <br> processes. Ensemble averages - mean function, auto-correlation function, <br> auto-covariance function. Stationary processes - strict-sense stationary <br> (SSS) process and wide-sense stationary (WSS) process. | $\mathbf{6}$ |
| $\mathbf{5}$ | Markov Processes - Markov chains - Markov property, transition <br> probability matrix, state-diagram. Processes with independent <br> increments - Poisson process. Modeling (applications of Markov chains <br> in Bio-informatics). Brownian motion - simple random walk. | $\mathbf{6}$ |
| $\mathbf{6}$ | Clustering: Definition and meaning, similarity and distance measures, <br> outliers. Clustering algorithms: hierarchical (agglomerative \& divisive) <br> and partitioning (k-means \& k-medoids). Clustering large databases, <br> clustering with categorical attributes, comparison. | $\mathbf{1 1}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. Ronald E. Walpole, Raymond H. Myers, Sharon L. Myers and Keying E. Ye: `’Probability and statistics for engineers and scientists', Pearson, Nineth edition, 2011.
2. T. Veerarajan: "'Probability, statistics and random processes", Tata McGraw-Hill, Third edition, 2008.
3. M. H. Dunham: "'Data mining: Introductory and advanced topics", Pearson, 2012.

## Suggested Reference Book(s):

1. Wayne W. Daniel: "Biostatistics: A foundation for analysis in the health sciences", John Wiley \& Sons, Nineth edition, 2008.
2. Jay L. Devore: "Probability and statistics for engineering and the sciences", Cengage Learning, Eight edition, 2011.
3. W. J. Ewens and G. R. Grant: "Statistical methods in bioinformatics", Springer 2001.
4. Alan Agresti and Barbara Finlay, "Statistical methods for the social sciences", Pearson prentice hall, Fourth edition, 2009.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/102101056
2. Link to topics related to course:
i. https://nptel.ac.in/courses/102101056/11
ii. https://nptel.ac.in/courses/102106051/28
iii. https://nptel.ac.in/courses/111102014/
iv. https://nptel.ac.in/courses/106108057/module14/ lecture34.pdf

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage /Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1. | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2. | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3 | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4 | Teaching Assessment | 25 | Entire <br> Semeste <br> r | Assignment (1) - 5 <br> Quizzes (2) - 15 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes (Biostatistics ) | ì | Ò | è | $\underset{i}{t}$ | in | Oi | $\hat{O}$ | $\stackrel{\infty}{0}$ | $\hat{\theta}$ | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | 쿨 | $\frac{\mathrm{T}}{1}$ | 迺 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 2 | 2 | 2 | 2 | 2 | 3 | 2 | 1 | 3 | 0 | 2 | 3 | 2.0 |
| CO-2 | 2 | 2 | 1 | 2 | 1 | 1 | 2 | 1 | 3 | 0 | 2 | 3 | 1.7 |
| CO-3 | 3 | 1 | 1 | 2 | 1 | 3 | 1 | 1 | 1 | 0 | 2 | 2 | 1.5 |
| CO-4 | 2 | 3 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | 0 | 1 | 2 | 1.3 |
| CO-5 | 2 | 2 | 2 | 1 | 3 | 1 | 1 | 1 | 1 | 0 | 1 | 2 | 1.4 |
| CO-6 | 3 | 2 | 3 | 2 | 3 | 3 | 2 | 1 | 3 | 2 | 2 | 3 | 2.4 |
| Average | 2.3 | 2.0 | 1.7 | 1.7 | 2.0 | 2.0 | 1.5 | 1.0 | 2.0 | 0.3 | 1.7 | 2.5 |  |

## Biostatistics Lab

COURSE CODE: 18B12MA481
COURSE CREDITS: 1
CORE/ELECTIVE: CORE
L-T-P: 0-0-2
Pre-requisite: Basic knowledge of Excel and SPSS.

## Course Objectives:

1. To develop computer programs for various probability and statistical concepts/procedures.
2. To execute and perform fundamental and specific statistical tests using computer software.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO 1 | Write and execute the programs to calculate correlation and <br> regression coefficients. | Familiarity and <br> Usage |
| CO 2 | Write and execute the programs to calculate least squares estimates. | Assessment |
| CO 3 | Write and execute the programs to perform run tests, signed-rank <br> tests, Wilcoxon test, Kruskal-Wallis and Friedman's test. | Usage |
| CO 4 | Write and execute the programs to obtain probability distributions <br> for Poisson's process. | Usage |
| CO 5 | Write and execute the programs to obtain probability distributions <br> for Markov chains | Assessment |
| CO 6 | Write and execute the programs for clustering and applications. | Usage |

## List of Experiments

| S.No | Description | Hours |
| :---: | :--- | :---: |
| 1 | To write a program to calculate correlation and simple linear regression <br> coefficients. | 2 |
| 2 | To write a program to calculate least squares estimates for linear regression <br> using method of least squares/normal equations. | 2 |
| 3 | To write a program to calculate least squares estimates for multivariate linear <br> regression coefficients, using matrix method. | 2 |


| 4 | To write a program to calculate least squares estimates for multivariate <br> polynomial regression coefficients. | 2 |
| :---: | :--- | :---: |
| 5 | To write a program to perform Run test for randomness for given data. | 2 |
| 6 | To write a program to perform Sign test and Signed-rank for one sample and <br> two samples for given data. | 2 |
| 7 | To write a program to perform and Wilcoxon test (Mann-Whitney test) test for <br> given data. | 2 |
| 8 | To write a program to perform Kruskal-Wallis test and Friedman's test for given <br> data. | 2 |
| 9 | To write a program to obtain probability distribution for Poisson process for <br> given arrival rate and time-interval with a specified detecting probability. | 2 |
| 10 | To write a program to obtain one-step and n-step transition probability <br> distributions for a given homogeneous Markov chain. | 2 |
| 11 | To write a program to obtain steady state probability distribution for a given <br> homogeneous Markov chain with n states. | 2 |
| 12 | To write a program for hierarchical agglomerative (Bottom-up) clustering and <br> display results in the form of a dendrogram. | 2 |
| 13 | To write a program for hierarchical divisive (Top-down) clustering and display <br> results in the form of a dendrogram. | 2 |
| 14 | To write a program to demonstrate partitioning clustering using k-means <br> algorithm. | 2 |
| 15 | To write a program to demonstrate partitioning clustering using k kedoids <br> algorithm. | 2 |
| Total Lab hours | 30 |  |

## Suggested/Resources:

1. Andy Field: Discovering Statistics Using IBM SPSS Statistics, 4th Edition, 2013, Sage Publications
2. Norman \& Streiner: Biostatistics-The Bare Essentials with SPSS, $4^{\text {th }}$ Edition, People's Medical Publishing House USA Ltd.
3. http://textofvideo.nptel.ac.in/110105060/lec32.pdf
4. https://nptel.ac.in/courses/106108057/module14/lecture34.pdf
5. https://nptel.ac.in/courses/111102014/

## Evaluation Scheme:

| 1 | Mid Sem. Evaluation | 20 Marks |
| :--- | :--- | :--- |
| 2 | End Sem. Evaluation | 20 Marks |
| 3 | Attendance | 15 Marks |
| 4 | Lab Assessment | 45 Marks |
|  | Total | 100 marks |

Course Outcomes (COs) contribution to the Programme Outcomes(POs)

| CO/PO | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 | PO9 | PO10 | PO11 | PO12 | Average |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: |
| CO1 | 2 | 2 | 2 | 2 | 2 | 3 | 2 | 1 | 3 | 0 | 2 | 3 | 2.0 |
| CO2 | 2 | 2 | 1 | 2 | 1 | 1 | 2 | 1 | 3 | 0 | 2 | 3 | 1.7 |
| CO3 | 3 | 1 | 1 | 2 | 1 | 3 | 1 | 1 | 1 | 0 | 2 | 2 | 1.5 |
| CO4 | 2 | 3 | 1 | 1 | 2 | 1 | 1 | 1 | 1 | 0 | 1 | 2 | 1.3 |
| CO5 | 2 | 2 | 2 | 1 | 3 | 1 | 1 | 1 | 1 | 0 | 1 | 2 | 1.4 |
| CO6 | 3 | 2 | 3 | 2 | 3 | 3 | 2 | 1 | 3 | 2 | 2 | 3 | 2.4 |
| Average | 2.3 | 2.0 | 1.7 | 1.7 | 2.0 | 2.0 | 1.5 | 1.0 | 2.0 | 0.3 | 1.7 | 2.5 |  |

## Optimization Techniques

## COURSE CODE: 10B1WMA731

COURSE CREDITS: 3
CORE/ELECTIVE: ELECTIVE
L-T-P: 3-0-0
Pre-requisite: None

## Course Objectives:

1. To understand the theory of optimization methods and algorithms developed for solving various types of optimization problems.
2. Provide students with the basic mathematical concepts of optimization.
3. Provide students with the modeling skills necessary to describe and formulate optimization problems.
4. Provide students with the skills necessary to solve and interpret optimization problems in engineering.
5. To apply the mathematical results and numerical techniques of optimization theory to concrete Engineering problems.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Solve linear programming problems by different methods. | Familiarity |
| CO-2 | Understand duality and dual simplex method. | Familiarity <br> Assessment |
| CO-3 | Understand assignment problem and method for solving it. | Familiarity |
| CO-4 | Understand transportation model and finding solution of transportation <br> problem. | Familiarity |
| CO-5 | Solve Integer programming problems by different methods. | Usage |
| CO-6 | Solve nonlinear programming problem by Lagrangian multiplier <br> method. | Assessment |
| CO-7 | Learn about KT conditions for solving NLPP. | Familiarity |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :--- | :--- | :--- |


| $\mathbf{1}$ | Linear Programming Problems(LPP): Definition of LPP, Simplex <br> Method, Artificial Variable Method, Two Phase Method, Charnes' <br> Big-M Method, Sensitivity Analysis, Revised Simplex Method | $\mathbf{1 0}$ |
| :---: | :--- | :---: |
| $\mathbf{2}$ | Auality, Dual Simplex Method | $\mathbf{5}$ |
| $\mathbf{3}$ | Transportation Problems: Introduction to Transportation Model, <br> Matrix Form of TP, Applications of TP Models, Basic Feasible Solution <br> of a TP, Degeneracy in TP, Formation of Loops in TP, Solution <br> Techniques of TP, Different Methods for Obtaining Initial Basic <br> Feasible Solutions viz. Matrix Minima Method, Row Minima Method, <br> Column Minima Methods, Vogel's Approximation Method. Techniques <br> for Obtaining Optimal Basic Feasible Solution | $\mathbf{9}$ |
| $\mathbf{4}$ | Integer Linear Programming Problems: Integer Linear Programming <br> Problems, Mixed Integer Linear Programming Problems, Cutting Plane <br> Method, Branch and Bound Method | $\mathbf{6}$ |
| $\mathbf{5}$ | Introduction to NLP : Definition of NLP, Convex Programming <br> Problems, Quadratic Programming Problems, Wolfe's Method for <br> Quadratic Programming Problem | $\mathbf{4}$ |
|  | Kuhn-Tucker Conditions, Geometrical Interpretation of KT-Conditions, <br> KT-points etc | $\mathbf{4}$ |
| Total lectures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. Taha, H.A.: Operations Research- An Introduction, New York, Macmillan, 1992.
2. Harvey M. Wagner: Principles of Operations Research with Applications to Managerial Decisions, Prentice Hall of India Pvt. Ltd 1975.

## Suggested Reference Book(s):

1. Hadley, G.: Linear Programming, Massachusetts: Addison- Wesley, 1962.
2. Hiller, F.S.and Lieberman G.J.: Introduction to Operations Research, San Francisco: Holden-Day, 1995.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111107104/
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111107104/6
ii. https://nptel.ac.in/courses/111107104/7
iii. https://nptel.ac.in/courses/111104027/
iv. https://nptel.ac.in/courses/111102012/

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (1) - 5 <br> Quizzes (1) - 15 <br> Attendance - 5 |

Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes <br> (Optimization <br> Techniques |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | $\mathbf{O}$

## Linear Programming and Applications

COURSE CODE: 10B1WMA832
COURSE CREDITS: 3
CORE/ELECTIVE: ELECTIVE
L-T-P: 3-0-0

Pre-requisite: None

## Course Objectives:

1. Provide students with the basic mathematical concepts of linear programming problems.
2. Provide student to formulate the LPP and conceptualize the feasible region.
3. Solve the LPP with two variables using graphical and simplex method.
4. Provide students to analyze the sensitivity of a decision variable.
5. Understand the concept of an objective function, a feasible region, and a solution set of an optimization problem.
6. Write down the dual linear programming problem.

## Course Outcomes:

| S.No. | Course Outcomes | Level of <br> Attainment |
| :---: | :--- | :---: |
| CO-1 | Understand basic terms and Solve linear programming problems by <br> graphical method. | Familiarity |
| CO-2 | Solve linear programming problems by simplex, big M and Two phase <br> methods. | Assessment |
| CO-3 | Understand duality and dual simplex method. | Familiarity |
| CO-4 | Understand assignment problem and method for solving it. | Familiarity |
| CO-5 | Understand transportation model and finding solution of transportation <br> problem. | Familiarity |
| CO-6 | Solve Integer programming problems by different methods. | Usage |
| CO-7 | Solving sequencing problems. | Usage |
| CO-8 | Understand game theory, CPM and PERT. | Familiarity |

## Course Contents:

| Unit | Contents | Lectures <br> required |
| :---: | :--- | :---: |
| $\mathbf{1}$ | Linear Programming Problems (LPP): Definition of LPP, <br> Mathematical formulations of LP Models, Graphical Solutions of Linear <br> Programming Problems (LPP) | $\mathbf{4}$ |
|  | Simplex Method, Artificial Variable Method, Two Phase Method, <br> Charnes' Big-M Method | $\mathbf{5}$ |
| $\mathbf{2}$ | Sensitivity Analysis, Revised Simplex Method, Duality, Dual Simplex <br> Method | $\mathbf{5}$ |
| $\mathbf{3}$ | Assignment Problems : Definition, Hungarian Method for AP <br> Transportation Problems : Introduction to Transportation Model, <br> Matrix Form of TP, Applications of TP Models, Basic Feasible <br> Solution of a TP, Degeneracy in TP, Formation of Loops in TP, <br> Solution Techniques of TP, Different Methods for Obtaining Initial <br> Basic Feasible Solutions viz. Matrix Minima Method, Row Minima <br> Method, Column Minima Methods, Vogel's Approximation Method. <br> Techniques for Obtaining Optimal Basic Feasible Solution | $\mathbf{4 2}$ |
| $\mathbf{4}$ | Integer Linear Programming Problems : Integer Linear Programming <br> Problems, Mixed Integer Linear Programming Problems, Cutting Plane <br> Method, Branch and Bound Method | $\mathbf{5}$ |
| $\mathbf{5}$ | Sequencing Problem: Johnsons Algorithm for n Jobs and Two <br> machines, n Jobs and Three Machines, 2 Jobs and m machines <br> problems | $\mathbf{3}$ |
| $\mathbf{6}$ | Game Theory: Concept of game; Two-person zero-sum game; Pure <br> and Mixed Strategy Games; Saddle point,Odds Method; Dominance <br> Method and Graphical Method for solving Mixed Strategy Game. <br> CPM and PERT- network diagram-Events and activities- project <br> planning reducing critical events and activities-critical path <br> calculations | $\mathbf{4}$ |
| $\mathbf{y y y y}$ (lures | $\mathbf{4 2}$ |  |

## Suggested Text Book(s):

1. Taha,H.A.: Operations Research- An Introduction, Macmillan, New York 1992.
2. Sharma S.D.: Operations Research, Kedar Nath Ram Nath, 2003.

## Suggested Reference Book(s):

1. Hadley, G.: Linear Programming, Massachusetts, Addison-Wesley, 1962.
2. Hiller, F.S. and Lieberman, G.J.: Introduction to Operations Research, Holden-Day, San Francisco 1995.

## Other useful resource(s):

1. Link to NPTEL course contents: https://nptel.ac.in/courses/111102012/
2. Link to topics related to course:
i. https://nptel.ac.in/courses/111104027/
ii. https://nptel.ac.in/courses/109103021/
iii. https://nptel.ac.in/courses/111102012/29
iv. https://nptel.ac.in/courses/111102012/27

## Evaluation Scheme:

| S. No | Exam | Marks | Duration | Coverage / Scope of <br> Examination |
| :---: | :--- | :--- | :--- | :--- |
| 1 | T-1 | 15 | 1 Hour. | Syllabus covered upto T-1 |
| 2 | T-2 | 25 | 1.5 Hours | Syllabus covered upto T-2 |
| 3. | T-3 | 35 | 2 Hours | Entire Syllabus |
| 4. | Teaching Assessment | 25 | Entire <br> Semester | Assignment (1) - 5 <br> Quizzes (1) - 15 <br> Attendance - 5 |

## Course Outcomes (COs) contribution to the Programme Outcomes (POs)

| Course outcomes <br> (Linear Programming and Applications) | Bi | ì | è | Ò | $\begin{aligned} & \text { n } \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & \text { Oi } \end{aligned}$ | $\hat{i}$ | $\stackrel{\infty}{0}_{\infty}^{\infty}$ | $\hat{i}$ | $0$ | 7 | $\frac{\mathrm{I}}{0}$ | 晨 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-1 | 3 | 3 | 2 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1.08 |
| CO-2 | 3 | 3 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0.92 |
| CO-3 | 3 | 3 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0.92 |
| CO-4 | 3 | 2 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 |
| CO-5 | 3 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 1 | 1 |
| CO-6 | 3 | 3 | 2 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0.83 |


| CO-7 | 3 | 3 | 2 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0.83 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CO-8 | 3 | 3 | 2 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0.92 |
| Average | 3 | 2.75 | 1.75 | 0.25 | 1 | 0 | 0.25 | 0 | 0.75 | 0 | 1 | 0.5 |  |

